上智大学数学談話会のお知らせ

日時: 2023年1月6日(金)17:30-18:30

場所:上智大学四谷キャンパス4号館3階4-398室

(Zoom によるオンライン配信あり)

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講演題目: $D_5^{(1)}$ and $D_6^{(1)}$ -Geometric Crystals and their ultra-discretizations

講演要旨: Let \mathfrak{g} be an affine Lie algebra with index set $I = \{0, 1, 2, \cdots, n\}$ and \mathfrak{g}^L be its Langlands dual. It is conjectured that for each Dynkin node $i \in I \setminus \{0\}$ the affine Lie algebra \mathfrak{g} has a positive geometric crystal whose ultra-discretization is isomorphic to the limit of certain coherent family of perfect crystals for \mathfrak{g}^L . In this talk, I will explain how we construct a positive geometric crystal for the affine Lie algebra $D_5^{(1)}$ corresponding to the Dynkin spin node k=5 and a positive geometric crystal for the affine Lie algebra $D_6^{(1)}$ corresponding to the Dynkin spin node k=6. Then I will explain how we define explicit 0-action on the level ℓ known perfect crystals and show that $\{B^{k,l}\}_{l\geq 1}$ is a coherent family of perfect crystals with limit $B^{k,\infty}$, k=5,6. I will also talk about how we show that for k=5,6, the ultra-discretization of $\mathcal{V}(D_k^{(1)})$ is isomorphic to $B^{k,\infty}$ as crystals which prove the conjecture in these cases.

